

The Gibbs Free Energy

Gibbs Function

$$G = U - TS + PV$$

$$dG = -S dT + V dP$$

$$= \left(\frac{\partial G}{\partial T}\right)_P dT + \left(\frac{\partial G}{\partial P}\right)_T dP$$

Temperature Dependence

$$\left(\frac{\partial G}{\partial T}\right)_P = \frac{G-H}{T}$$

$$\left(\frac{\partial(G/T)}{\partial T}\right)_P = -\frac{H}{T^2}$$

Pressure Dependence

$$G(T,P) = G^\circ(T) + \int_{P^\circ}^P V dP$$

Liquids/Solids: $G(T,P) \approx G^\circ(T)$

Ideal Gases: $G(T,P) = G^\circ(T) + nRT \ln P$

Chemical Potential - Part 1

$$\mu(T,P) = \frac{G(T,P)}{n}$$

Liquids/Solids: $\mu(T,P) \approx \mu^\circ(T)$

Ideal Gases: $\mu(T,P) = \mu^\circ(T) + RT \ln P$

Real Gases: $\mu(T,P) = \mu^\circ(T) + RT \ln (f/P^\circ)$

$$\ln\left(\frac{f}{P}\right) = \frac{1}{RT} \int_0^P (\bar{V} - \bar{V}_{id}) dP$$