

Problem Set 6

1. Suppose a gas has the following behavior:

$$\left(\frac{\partial U}{\partial V}\right)_T = 0$$

$$P(V - b) = RT$$

Calculate the following two quantities:

$$\left(\frac{\partial H}{\partial V}\right)_T$$

$$C_p - C_v$$

2. For Air, $\gamma = 1.40$. Which is the best model for an Air “molecule”:

An elastic sphere.

A rigid dumbbell.

A non-rigid dumbbell which vibrates and rotates.

3. Compare the Specific Heat of Ice with that calculated from the Law of Dulong-Petit. Explain any difference.

4. Read the article of Dulong and Petit and answer the following questions:

- What is the principle of Irvine and Crawford? Is their proposal supported experimentally?
- What do Dulong and Petit identify as a major cause of error in heat capacity measurements?
- How did Dulong and Petit overcome deal with this source of error in their heat capacity measurements?
- Do the measurements of heat capacity for Oxygen and Azote by Laroche and Berard deviate from the Law of Dulong and Petit? Explain.

4. The compression ratio in a diesel engine is 16:1; that is, the gas in the piston is compressed to 1/16 its original volume. Take C_p of Air to be 27 J/K mol independent of temperature. Assuming the compression stroke of a diesel engine to be reversible and adiabatic, calculate the temperature increase of Air in the cylinder during a compression stroke. (Assume the operating temperature is 350K.)

[Ans. 1202K]

5. One mole of an Ideal Gas is compressed Adiabatically from 0.100 MPa to 1.00 MPa. Initially the gas is at 27°C. The gas is diatomic with $C_v = 5/2 R$.
- Assume the compression is done in a single stage with a constant opposing pressure of 1.0 MPa.
 - Assume the compression is done reversibly.

For each case, compute the final temperature and Q, W, ΔU and ΔH .

[Ans. (a) 1072K, 0, 16.0 kJ/mol, 16.0 kJ/mol, 22.5 kJ/mol (b) 579K, 0, 5.80 kJ/mol, 5.80kJ/mol, 8.12 kJ/mol]

6. Suppose that a piece of metal with a volume of 100 cm³ is compressed adiabatically by a shock wave of 10⁵ atm to a volume of 90 cm³. Assume the compression occurs at a constant pressure of 10⁵ atm. Calculate ΔU and ΔH for the metal.
7. In an Ideal Gas undergoes a reversible polytropic expansion, the relation $PV^n = C$ holds throughout the process; where C and n are constants with $n > 1$. Calculate W for such an expansion if one mole of the gas expands from V_1 , where $T_1 = 300$ K, to V_2 , where $T_2 = 200$ K. Assume $n = 2$. If $C_v = (5/2)R$ for the gas, calculate ΔU , Q and ΔH for this change in state.
- [Ans. 830 kJ/mol, -2080 kJ/mol, -1250 kJ/mol, -2910 kJ/mol]