

Problem 2. Let $A = (a_{ij})$ be a matrix and (b_1, \dots, b_n) and (x_1, \dots, x_n) be vectors with real entries. Using Θ notation, describe the number of arithmetic operations in the algorithm

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for  $i = 1, \dots, n$ 
  for  $j = 1, \dots, i - 1$ 
     $x_i = b_i - a_{ij}x_j$ 
  end
   $x_i = b_i/a_{ii}$ 
end

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Let C be the # of arithmetic operations (flops).

$$C = \sum_{i=1}^n \left(\sum_{j=1}^{i-1} 2 + 1 \right) = \sum_{i=1}^n 2(i-1) + n$$

$$= 2 \sum_{i=1}^{n-1} i + n = 2 \frac{(n-1)n}{2} + n = n^2.$$

$$C = \Theta(n^2).$$

Problem 3. Give a recursive algorithm for computing na , where $n \in \mathbb{Z}^+$ and $a \in \mathbb{R}$.

$$n=1 \Rightarrow na = a$$

$$na = (n-1)a + a$$

procedure $na(n, a)$

if $n=1$ then

output = 1

else

output = $na(n-1, a) + a$

end

{output}.