

## Test 2

Problem	1	2	3	4	5	6	7	Score
Points								

NAME: \_\_\_\_\_

Solution Key

Show all your work for full credit. Calculators, the textbook, and lecture notes are not allowed.

Problem 1. Evaluate the integral Use integration by parts twice.

$$\begin{aligned}
 \int e^{2x} \sin x \, dx &= - \int e^{2x} (\cos x)' \, dx = -e^{2x} \cos x + 2 \int e^{2x} \cos x \, dx \\
 &= -e^{2x} \cos x + 2 \int e^{2x} (\sin x)' \, dx \\
 &= -e^{2x} \cos x + 2 e^{2x} \sin x - 4 \int e^{2x} \sin x \, dx. \\
 \Rightarrow 5 \int e^{2x} \sin x \, dx &= e^{2x} (2 \sin x - \cos x) + C \\
 \int e^{2x} \sin x \, dx &= \frac{e^{2x}}{5} (2 \sin x - \cos x) + C.
 \end{aligned}$$